

Intensity distribution of fringes

we know that during interference of waves between two sources

$$A^2 = a_1^2 + a_2^2 + 2a_1a_2 \cos \delta$$

If $a_1 = a_2 = a$ (which is generally the case)

$$\text{then } A^2 = a^2 + a^2 + 2a^2 \cos \delta$$

$$A^2 = 2a^2 [1 + \cos \delta]$$

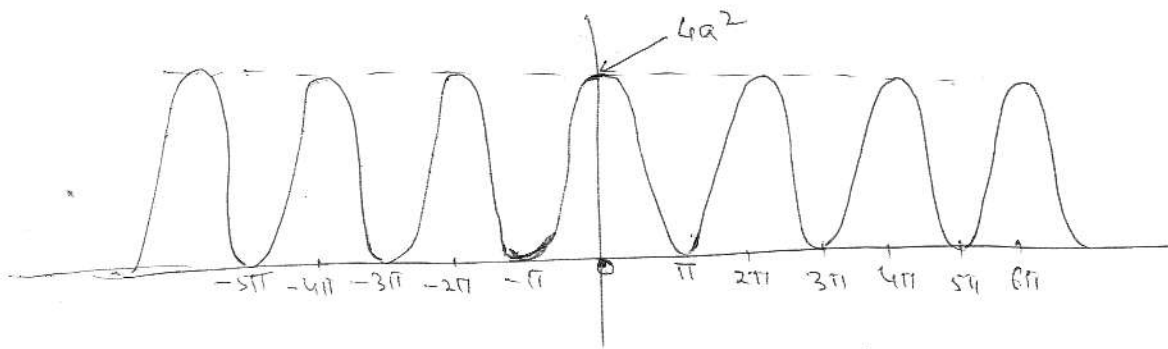
$$\Rightarrow I = 2a^2 (1 + \cos \delta)$$

At max at $\delta = 0, 2\pi, 4\pi, 6\pi \dots \cos \delta = 1$

$$\therefore I = I_{\max} = 2a^2 [1 + 1] = 4a^2$$

At minima at $\delta = \pi, 3\pi, 5\pi \dots \cos \delta = -1$

$$\therefore I = I_{\min} = 2a^2 [1 - 1] = 0$$



Note 1 If $a_1 \neq a_2$ then

$$I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \delta$$

where $I_1 = a_1^2$ and $I_2 = a_2^2$ are intensities due to individual sources

Note 2 Intensities from two sources are proportional to width of sources

$$\therefore \frac{I_1}{I_2} = \frac{w_1}{w_2} = \frac{a_1^2}{a_2^2}$$